

# Supporting Special Populations Through Instructional Routines

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#FosteringMPs  
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**MATH**  
**PRACTICES**

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#EPSOBO

@AmyLucenta

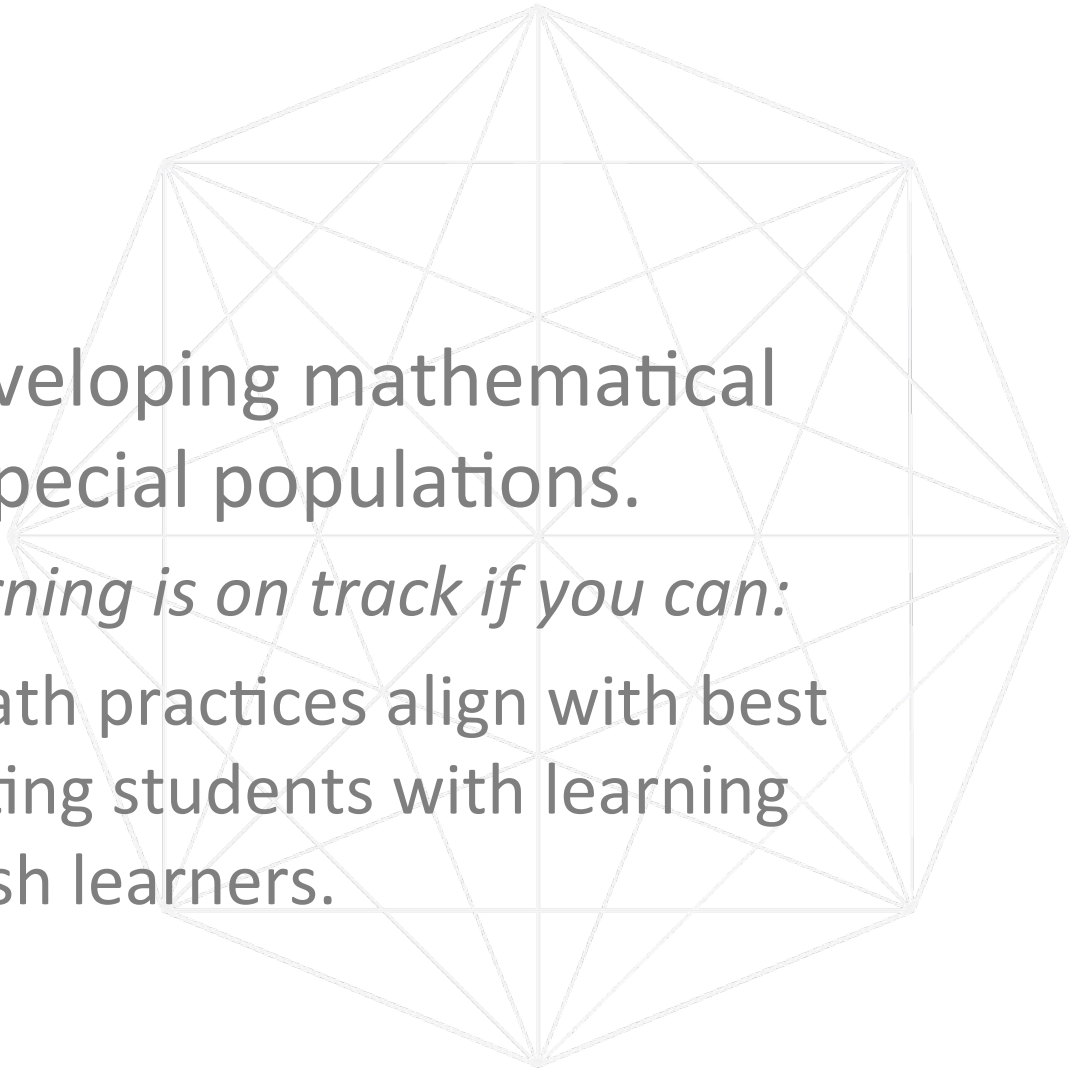
@GraceKelemanik

# Goal # 1

Understand how developing mathematical practices supports special populations.

*You will know your learning is on track if you can:*

- Describe how the math practices align with best practices for supporting students with learning disabilities and English learners.

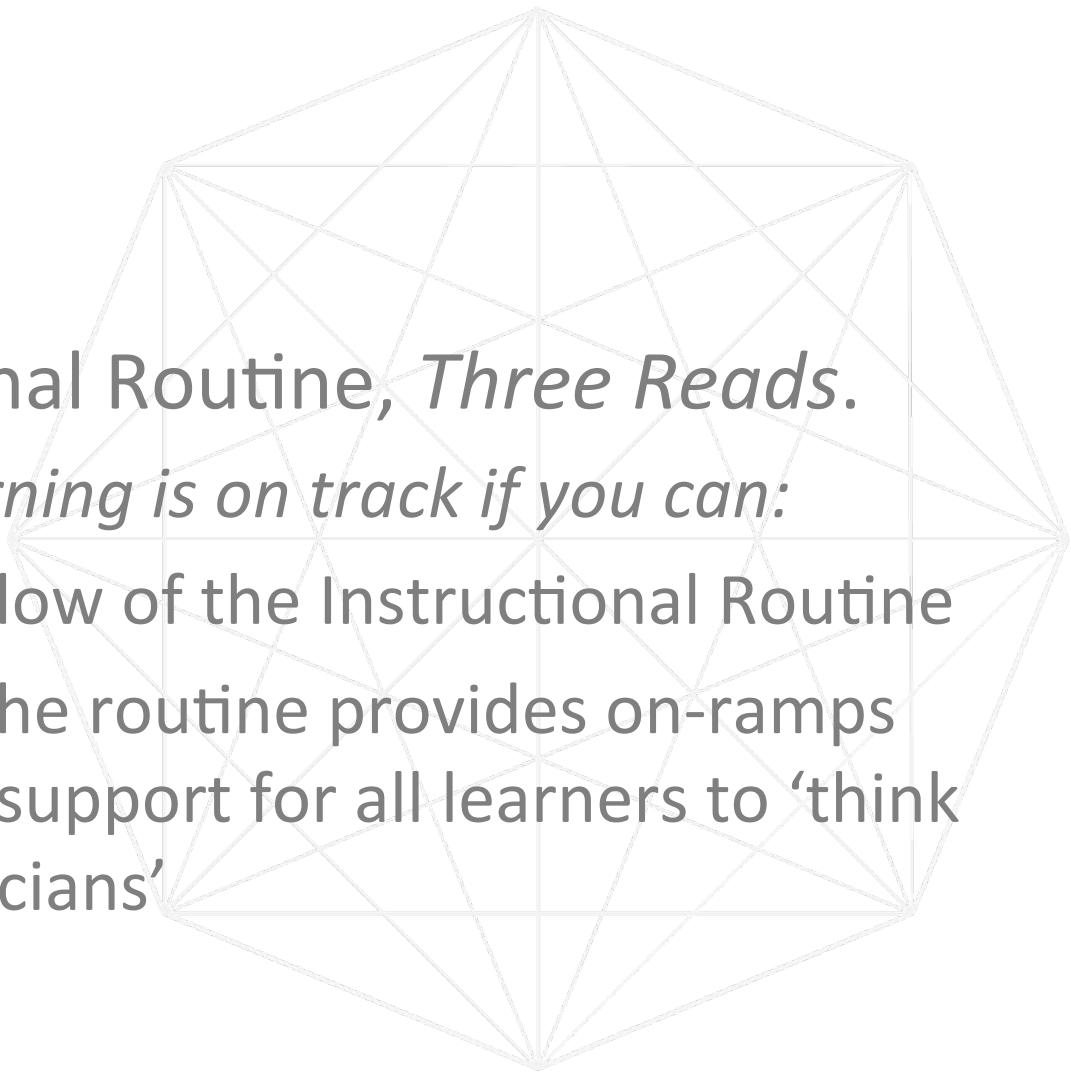


## Goal # 2

Learn the Instructional Routine, *Three Reads*.

*You will know your learning is on track if you can:*

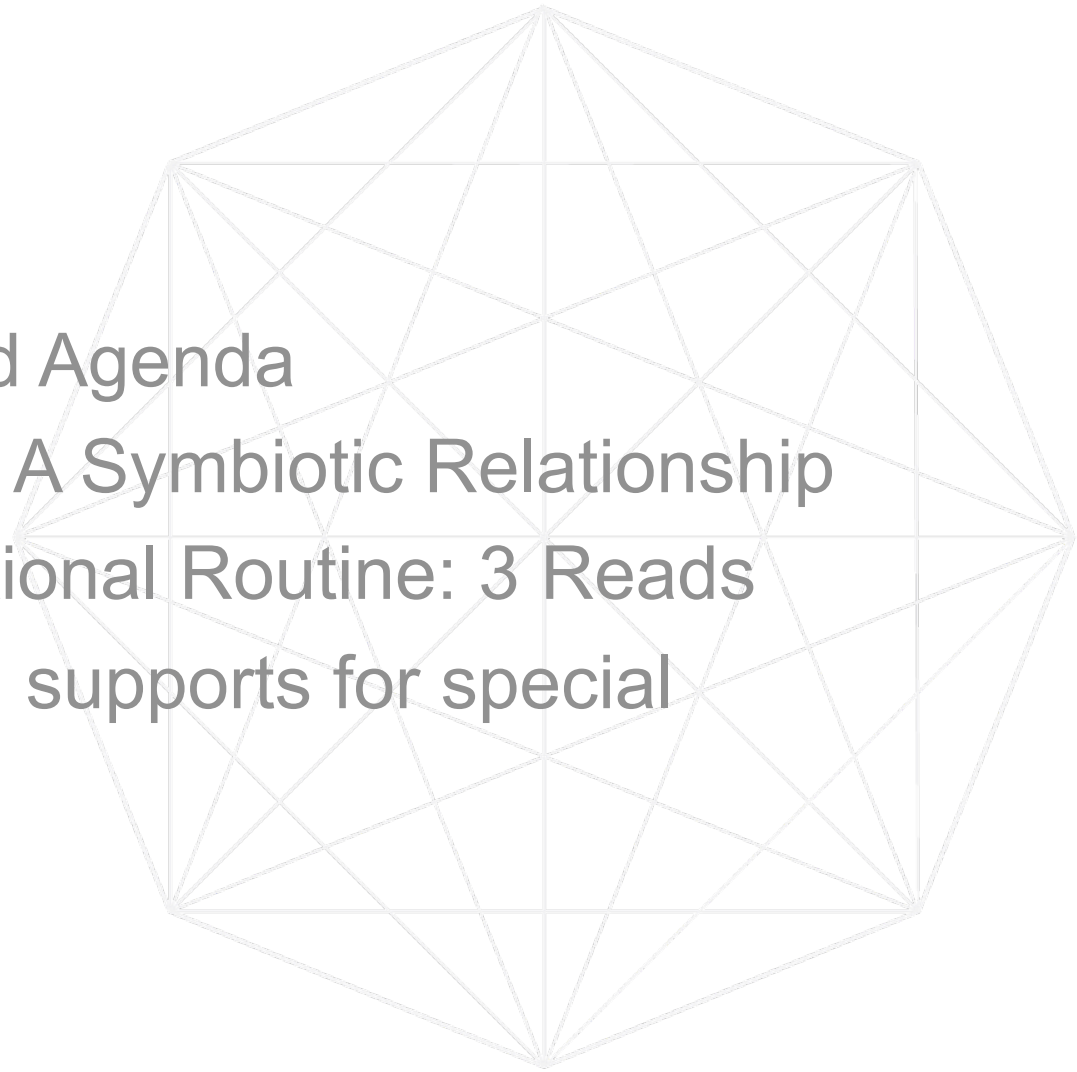
- Articulate the flow of the Instructional Routine
- Describe how the routine provides on-ramps and continued support for all learners to ‘think like mathematicians’





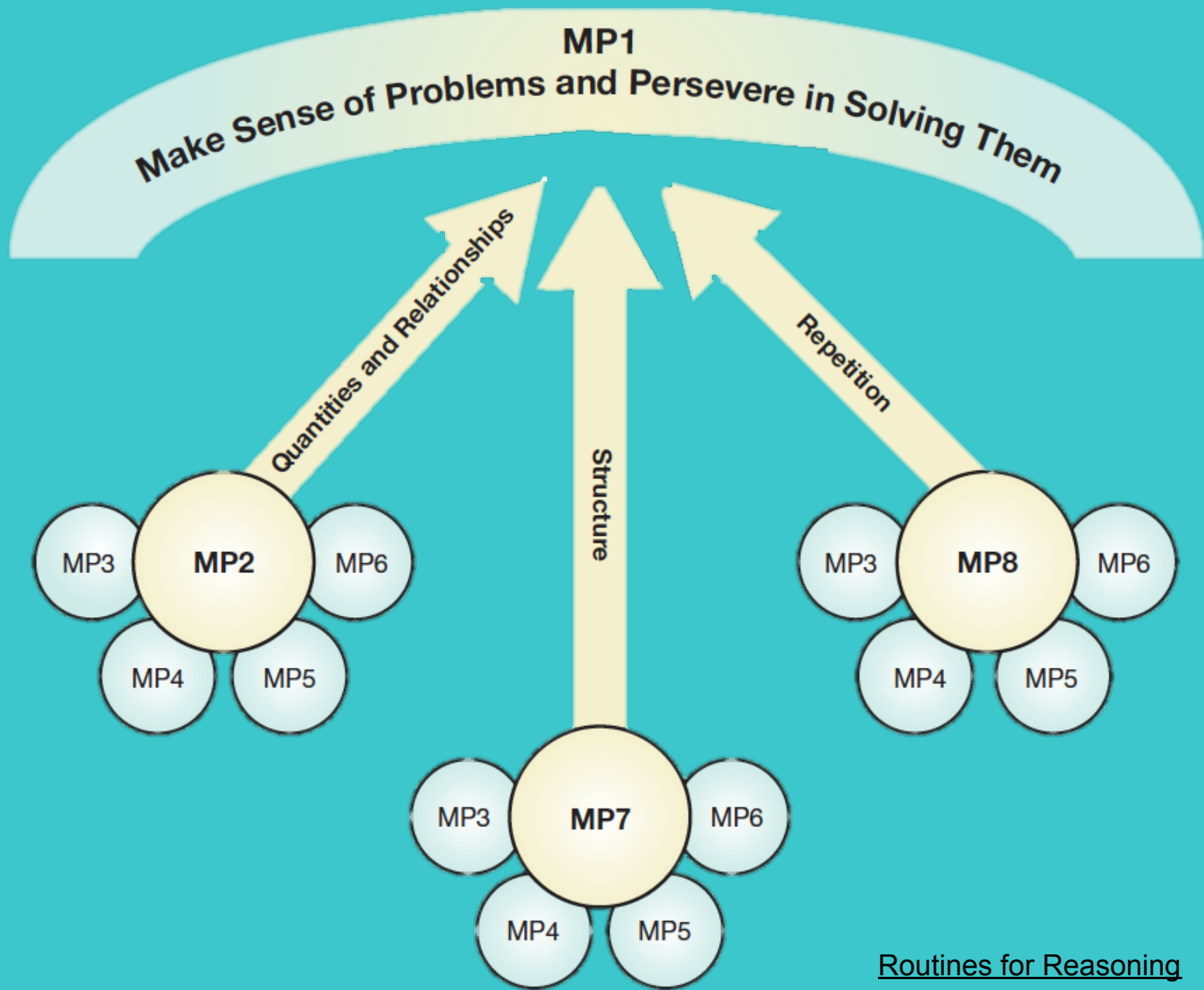
# Agenda

- Opening Goals and Agenda
- MPs and SpPops: A Symbiotic Relationship
- Explore an Instructional Routine: 3 Reads
- Articulate essential supports for special populations



# Standards for Mathematical Practice

- **MP1** Make Sense of Problems and Persevere in Solving Them
- **MP2** Reason Abstractly and Quantitatively
- **MP3** Construct Viable Arguments and Critique the Reasoning of Others
- **MP4** Model with Mathematics
- **MP5** Use Appropriate of Tools Strategically
- **MP6** Precision in Mathematics
- **MP7** Look for and Make Use of Structure
- **MP8** Look for and Express Regularity in Repeated Reasoning





# MATH PRACTICES

- a. An essential goal for all?*
- b. A critical support for special populations?.*

# MATH PRACTICES

**MP4**

Model

**MP8**

Repetition

**MP3**

Construct &  
critique

**MP7**

Structure

**MP2**

Reason  
quantitatively

**MP6**

Precision

**MP1**

Make sense &  
persevere

**MP5**

Tools



# MATH PRACTICES



# MATH PRACTICES









MP 1 MP 2 MP 3

MP 5  
MP 4

MP 8  
MP 7  
MP 6





# WORK WITHIN CONTEXTS

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MP1 MP2 MP4

# WORK WITHIN CONTEXTS

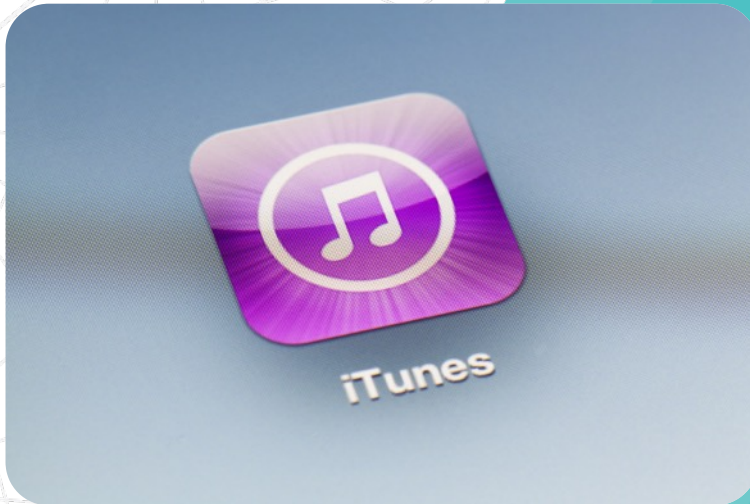
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$$\begin{array}{r} 25 \\ \times 9 \\ \hline \end{array}$$



# WORK WITHIN CONTEXTS

---



The background features a teal-colored mountain peak with a jagged top edge, set against a white background with a light gray wireframe grid. The grid consists of interconnected lines forming a series of triangles and polygons, creating a geometric pattern that resembles a snow-capped mountain or a crystalline structure. The teal mountain peak is positioned in the lower-left to center area, with its top edge following the jagged outline of the wireframe structure.

# COMMUNICATE IDEAS

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MP1 MP3 MP6

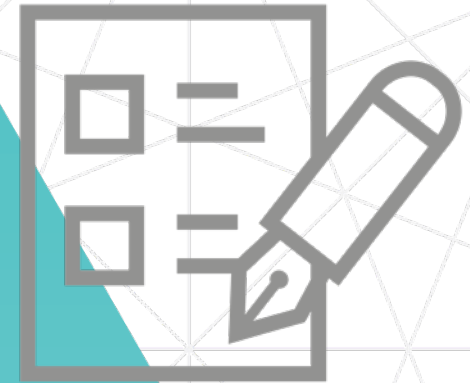
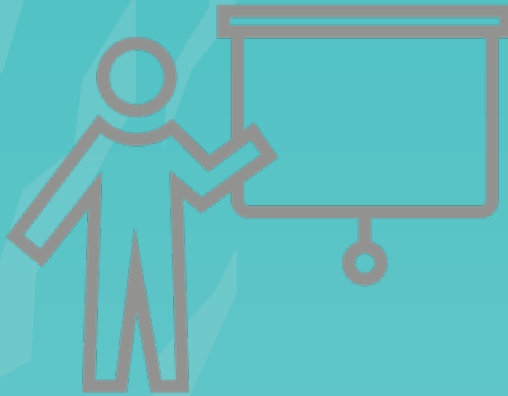
# COMMUNICATE IDEAS

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# COMMUNICATE IDEAS

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# CONNECT IDEAS & REPRESENTATIONS

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MP2 MP4 MP5 MP7



# CONNECT IDEAS & REPRESENTATIONS

$$\frac{5}{4}$$



five fourths



# CONNECT IDEAS & REPRESENTATIONS

---



# ABSTRACT & GENERALIZE

---

MP2 MP7 MP8

The background features a large teal-colored shape with a jagged, mountain-like top edge. This shape is overlaid on a light gray wireframe structure that consists of interconnected lines forming a complex, multi-faceted geometric pattern. The overall aesthetic is clean and modern, with a focus on geometric forms and abstract patterns.

# ABSTRACT & GENERALIZE

---

**MP2**  
Quantitative Reasoning

**MP7**  
Structural Thinking

**MP8**  
Repeated Reasoning

# MP1 PERSEVERANCE

**MP2**  
Quantitative Reasoning

**MP7**  
Structural Thinking

**MP8**  
Repeated Reasoning

# A SYMBIOTIC RELATIONSHIP



**TEACH MATH  
PRACTICES  
AUTHENTICALLY**

**SUPPORT  
SPECIAL  
POPULATIONS**

**SWLD**

**ELL**

**Work within contexts**

**Opportunities to communicate ideas**

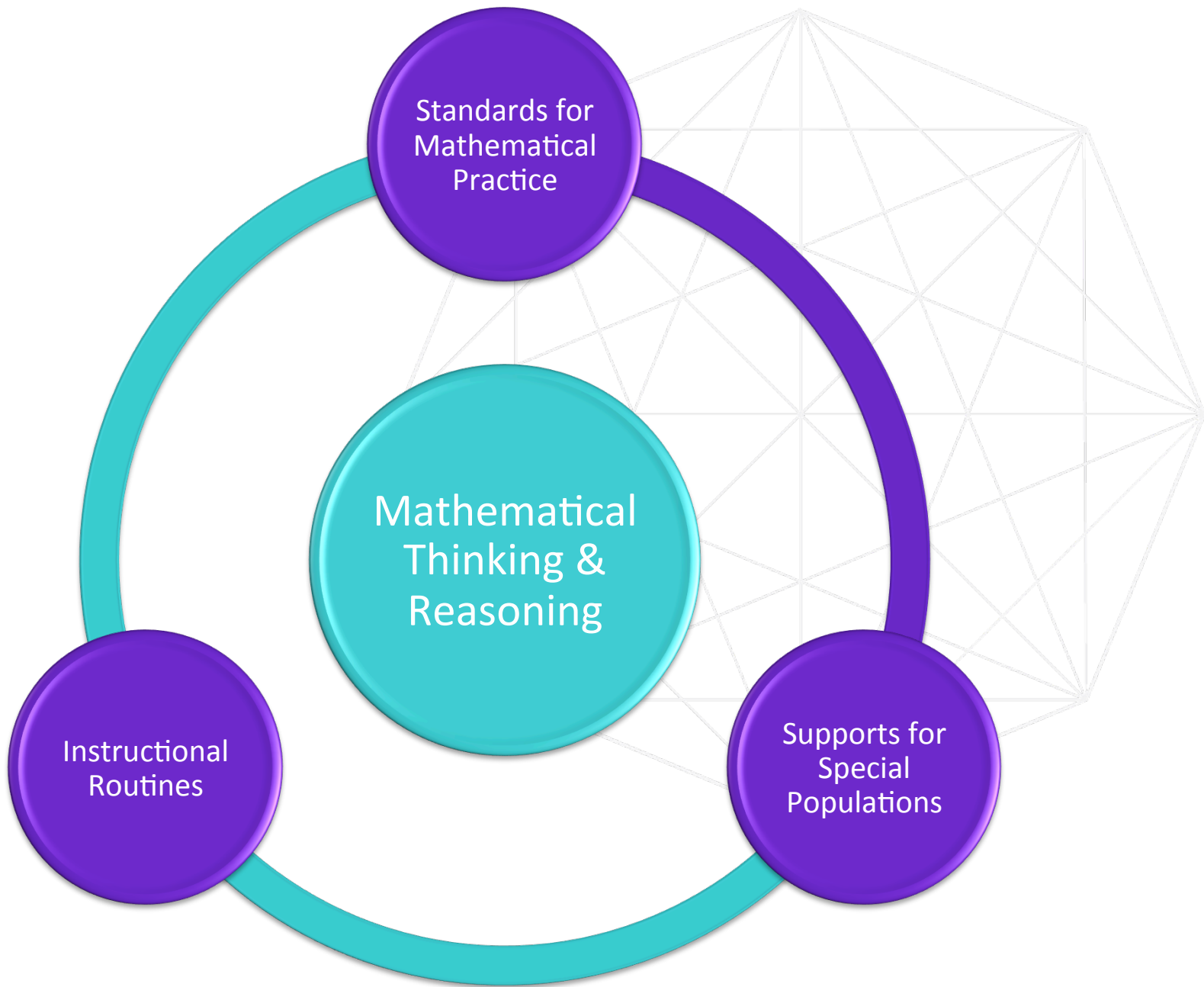
**Multisensory learning experiences**

**Connect ideas & representations**

**Opportunities for multiple strategies**

**Multiple practice opportunities for students to develop mathematical understanding**

**Carefully planned range & sequence of examples**



Standards for  
Mathematical  
Practice

Mathematical  
Thinking &  
Reasoning

Instructional  
Routines

Supports for  
Special  
Populations



**SWLD**

**ELL**

**Work within contexts**

**Opportunities to communicate ideas**

**Multisensory learning experiences**

**Connect ideas & representations**

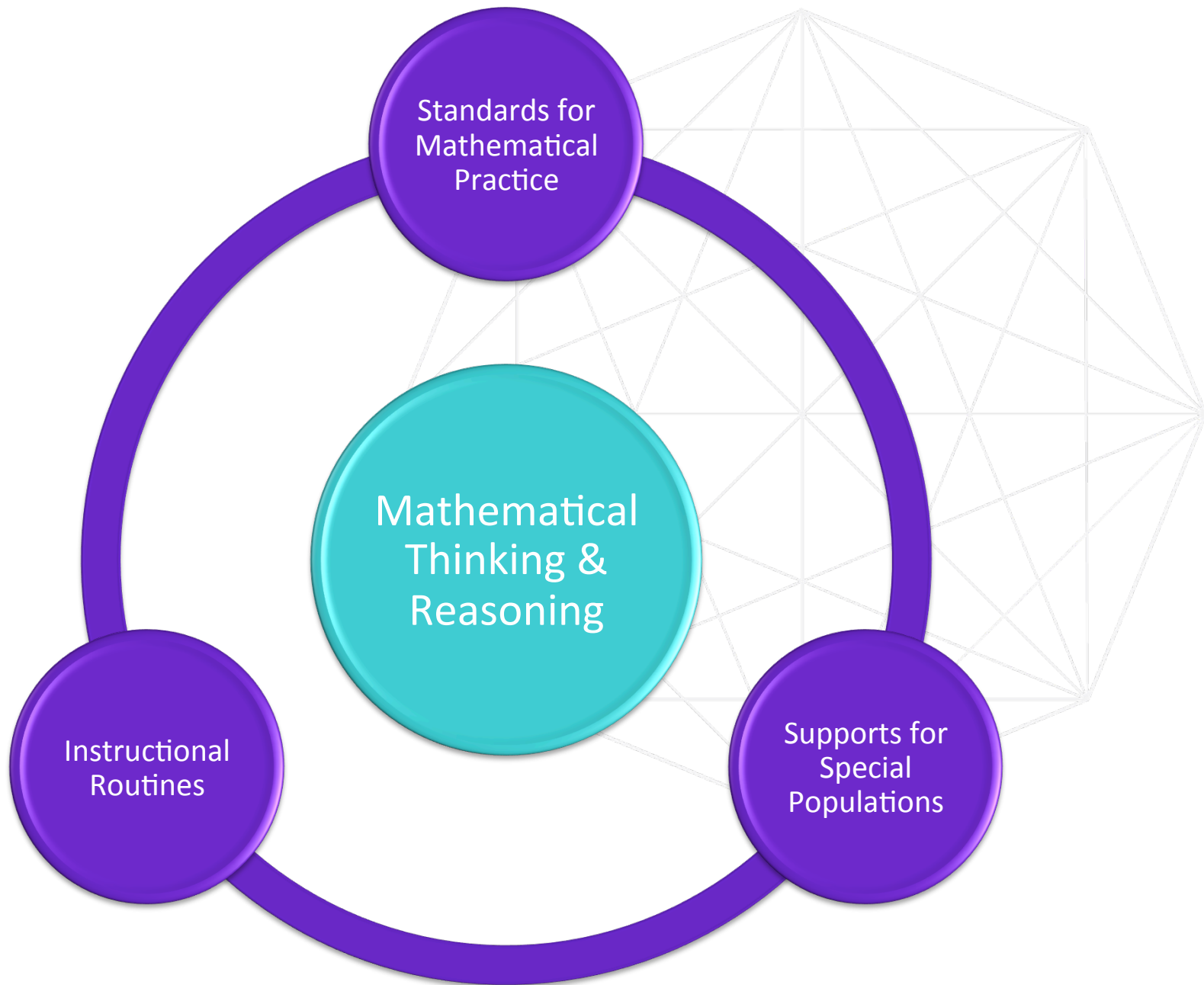
**Opportunities for multiple strategies**

**Multiple practice opportunities for students to develop mathematical understanding**

**Carefully planned range & sequence of examples**



**HOW ARE INSTRUCTIONAL ROUTINES  
SUPPORTS for  
SPECIAL POPULATIONS?**



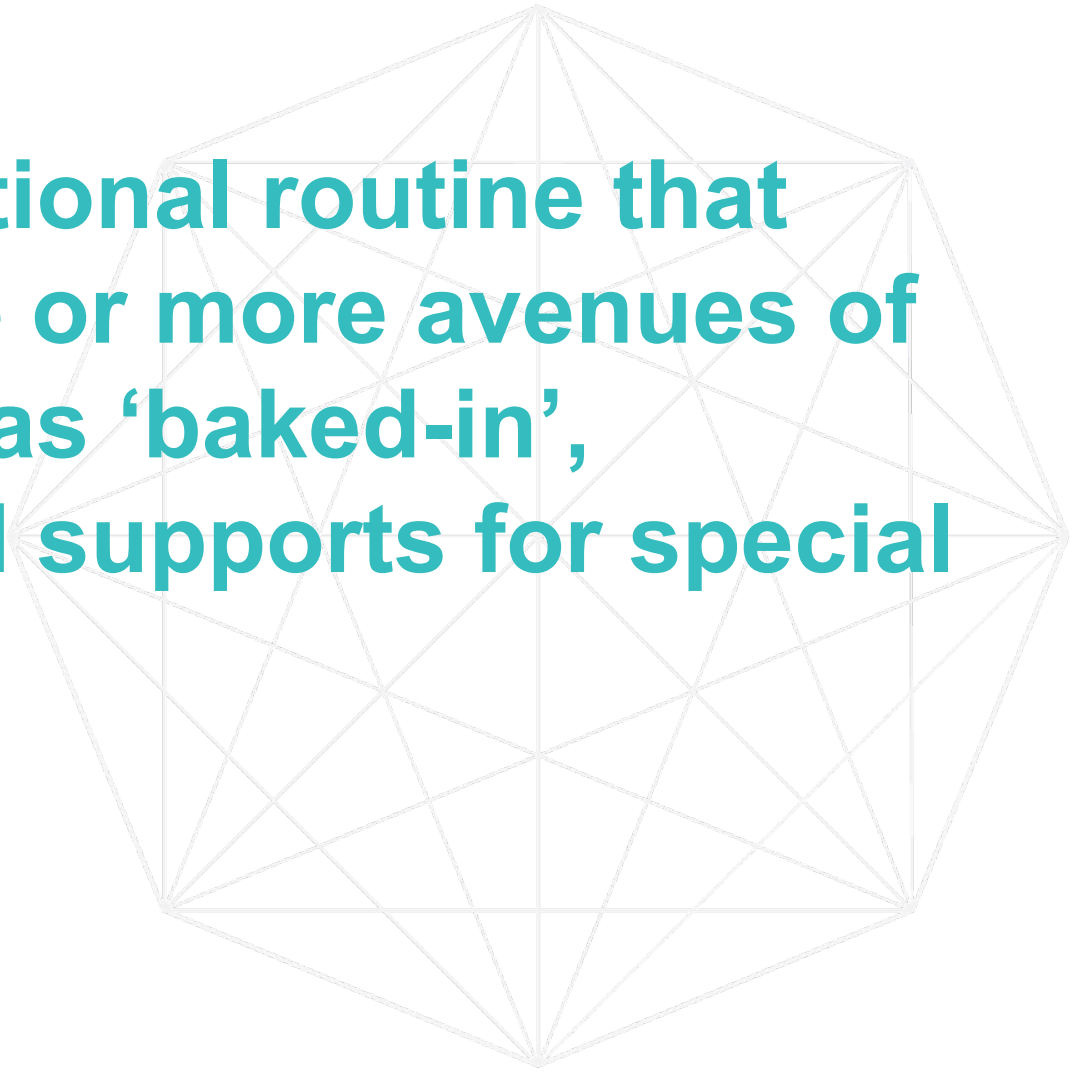
Standards for  
Mathematical  
Practice

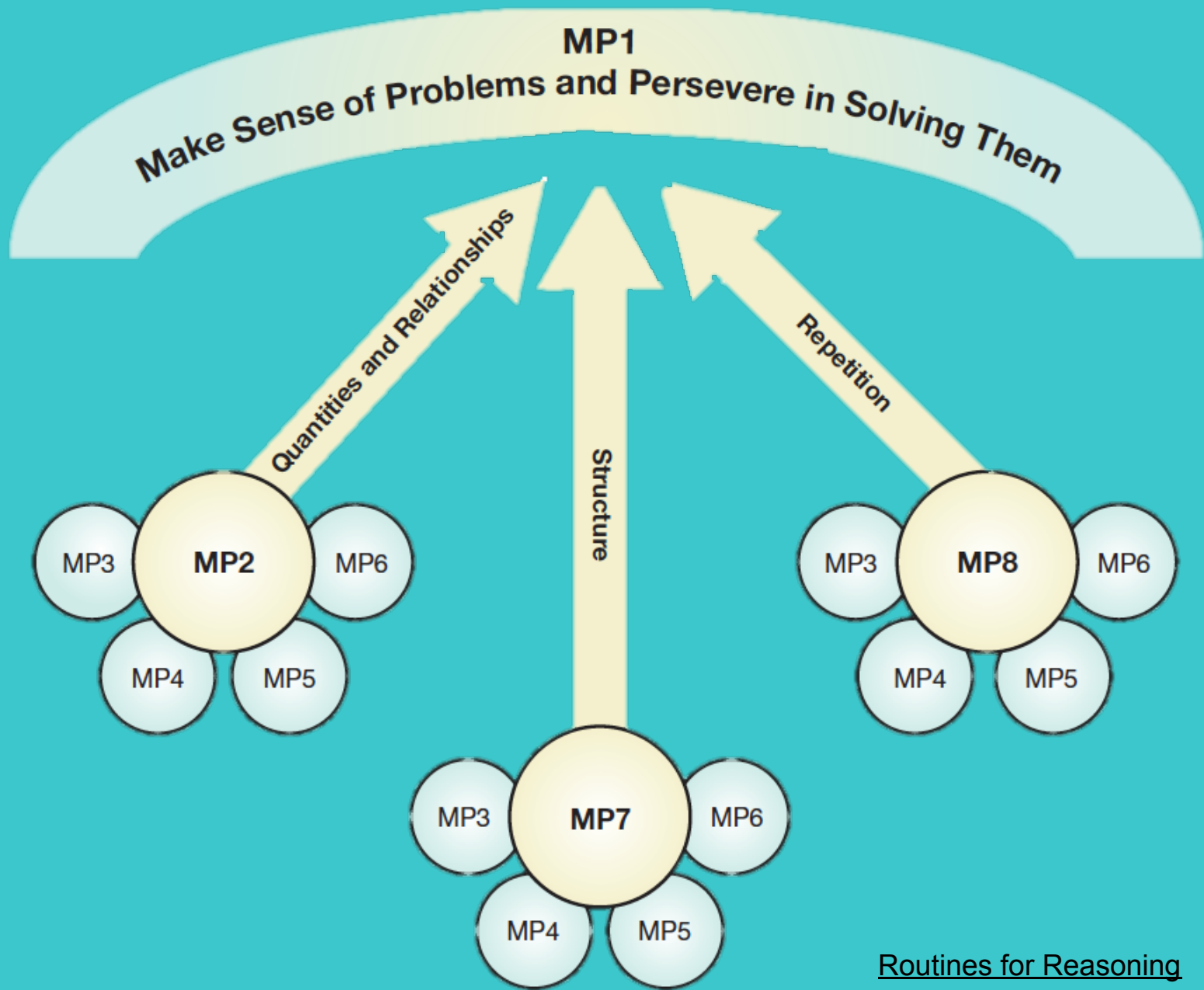
Mathematical  
Thinking &  
Reasoning

Instructional  
Routines

Supports for  
Special  
Populations

**So...an instructional routine that focuses on one or more avenues of thinking, and has 'baked-in', research-based supports for special populations...**

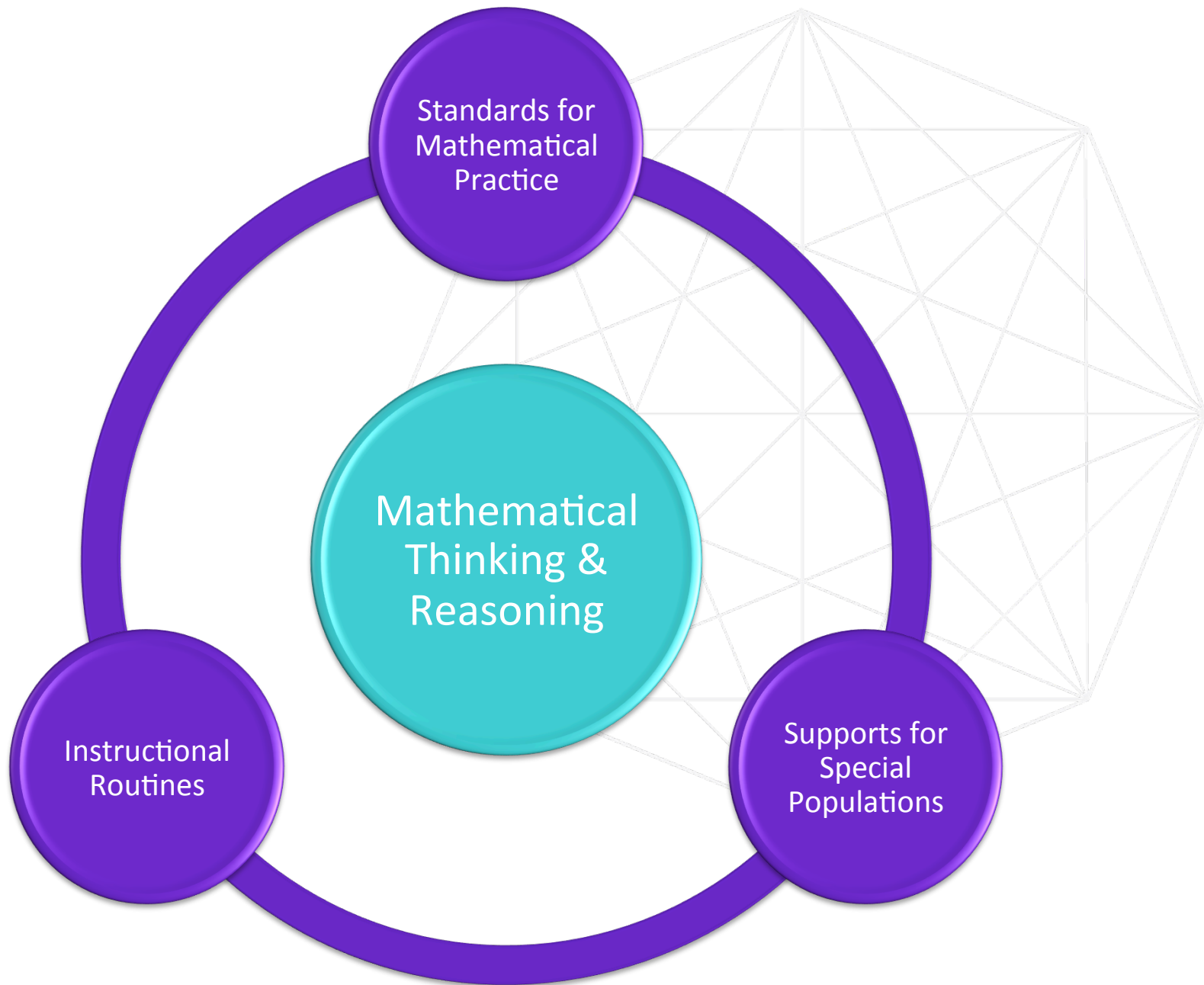




# Developing mathematical practices requires high leverage teaching practices

Instructional Routines embody  
NCTM effective teaching practices

and equitable practices for students,  
teachers, and districts.

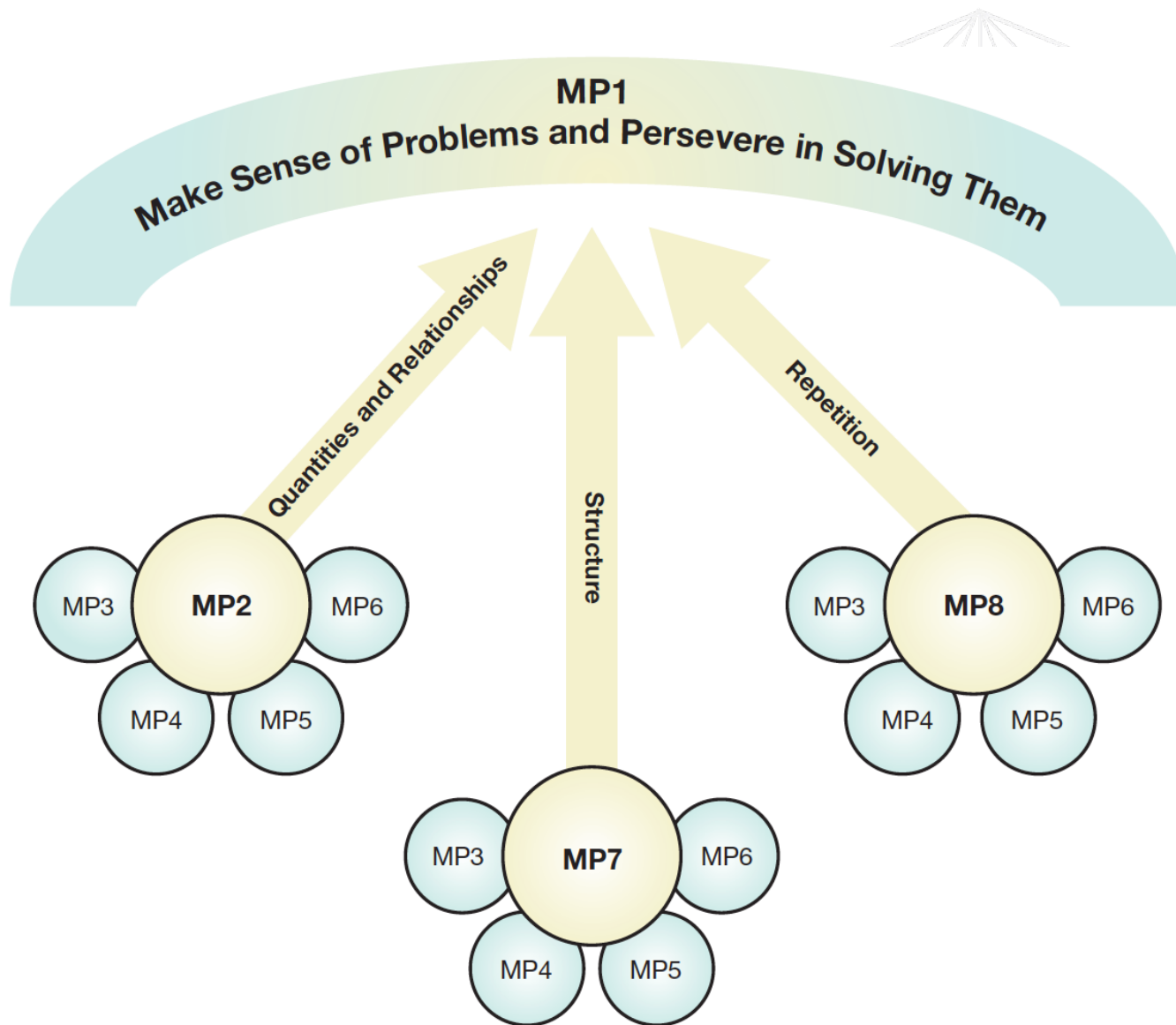


Standards for  
Mathematical  
Practice

Mathematical  
Thinking &  
Reasoning

Instructional  
Routines

Supports for  
Special  
Populations



**Figure 1.1** Diagram that shows the relationship of the practices to each other



# Three Reads Deep Dive

1. A few words on reading in Math
2. Experience the *Three-Reads* Instructional Routine x2
3. Unpack the *Three-Reads* Instructional Routine
4. Consider who this routine supports and how it supports them

A school bought some math books and 4 times as many science books. The cost of a math book was \$12 while a science book cost \$8. Altogether the school spent \$528. How many science books did the school buy?

$$4 \times 8 = 32$$

$$\begin{array}{r} 32 \overline{) 528} \\ \underline{32} \phantom{00} \\ 808 \\ \underline{192} \\ 16 \end{array}$$

16 Science Books

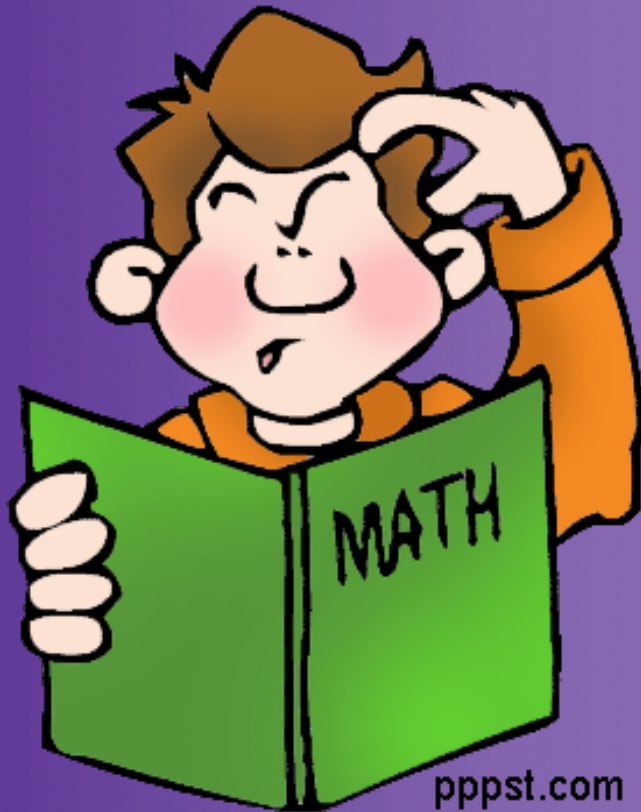
$$\begin{array}{r} 32 \\ \times 16 \\ \hline 192 \\ 320 \\ \hline 512 \end{array}$$

Instructions:

1. Solve the textbook task.
2. Analyze the student work.
3. Talk with a partner about how the student was thinking.



# Why is reading a math problem challenging for students?



pppst.com

I don't get it!



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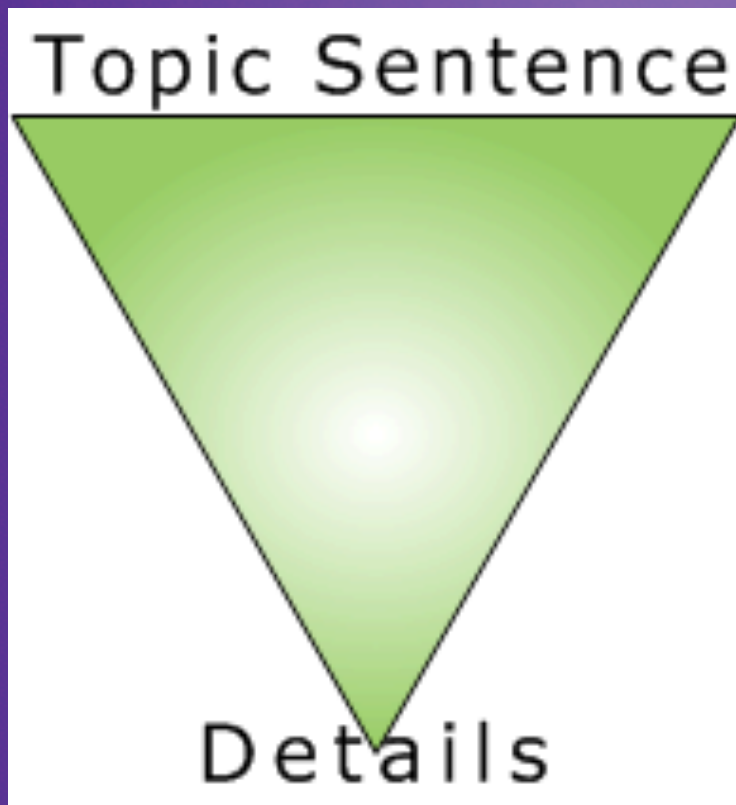


# Mathematicians read the problem more than once!

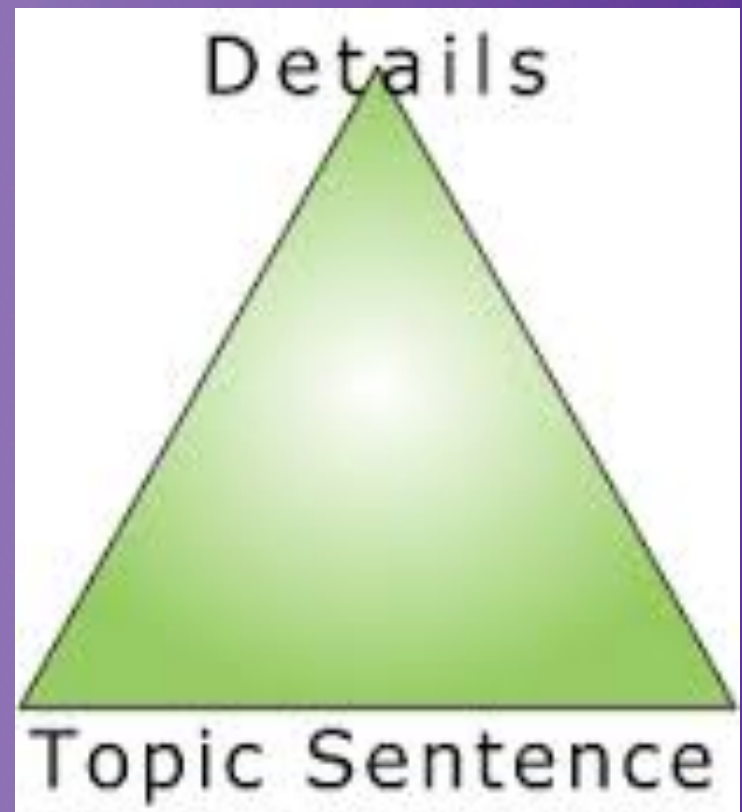


# Math problems are written differently

## PARAGRAPH STRUCTURE



## MATH WORD PROBLEMS



D  
E  
T  
A  
I  
L  
S

*A school bought some math books and 4 times as many science books. The cost of a math book was \$12 while a science book cost \$8.*

*Altogether the school spent \$528. How many science books did the school buy?*

P  
u  
r  
p  
o  
s  
e



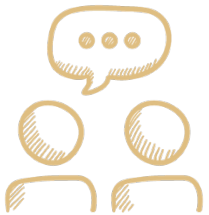
# Read the Problem 3 Times



**1<sup>st</sup> Read** What is the problem about?



**2<sup>nd</sup> Read** What is the question?



**3<sup>rd</sup> Read** What information is important?



# What information do mathematicians think important?

Quantities & Relationships





# What's a Quantity?

- A Quantity is something you can count or measure
  - The number of...
  - The amount of...
- It answers the questions:
  - How many?
  - How much?

What are the quantities in this problem?

*A school bought some math books and 4 times as many science books. The cost of a math book was \$12 while a science book cost \$8. Altogether the school spent \$528. How many science books did the school buy?*



# What's a Relationship?

- A Relationship describes a comparison between two quantities.
- The number of... is (relationship) the number of ....

Quantity



Quantity



What are the relationships between quantities in this problem?

*A school bought some math books and 4 times as many science books. The cost of a math book was \$12 while a science book cost \$8. Altogether the school spent \$528. How many science books did the school buy?*

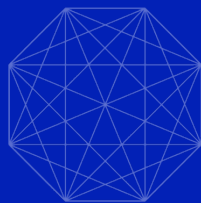




# Three Reads

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An Instructional Routine to Develop  
Reading Like a Mathematician



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# Lesson Goal

Learn to “read like a mathematician”.  
Pay attention to quantities in the  
problem statement.

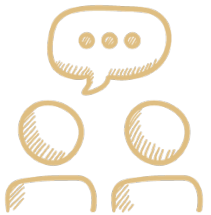
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# 1<sup>st</sup> Read

What is the  
problem  
about?



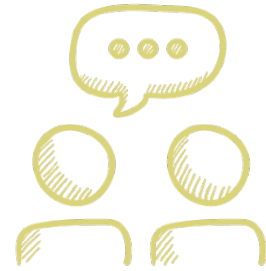


# 2<sup>nd</sup> Read



# What's the Question?

Rick keeps his trading cards in a box. Rick's uncle gave him 6 packs of 8 trading cards to add to his box. Rick found that 29 of the trading cards from his uncle were different than any of the cards he already had in the box. The rest of the trading cards from his uncle were the same as those he already had. How many of the trading cards from his uncle were the same as those Rick already had in his box?

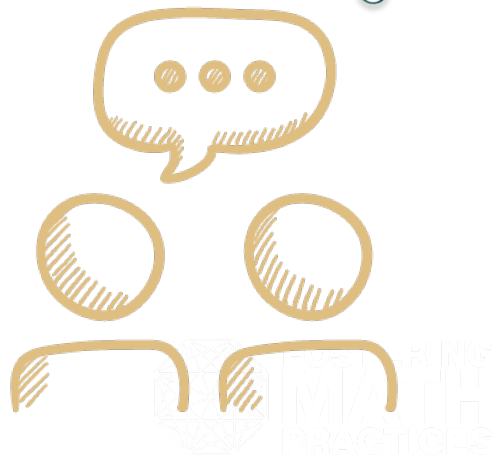


**State the question in your own words.**

What quantity am I trying to find?

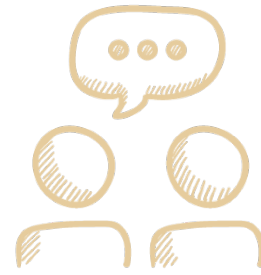
# 3<sup>rd</sup> Read

What's the  
important  
information?



# What's the Important Information?

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What are the important quantities?

The number of...

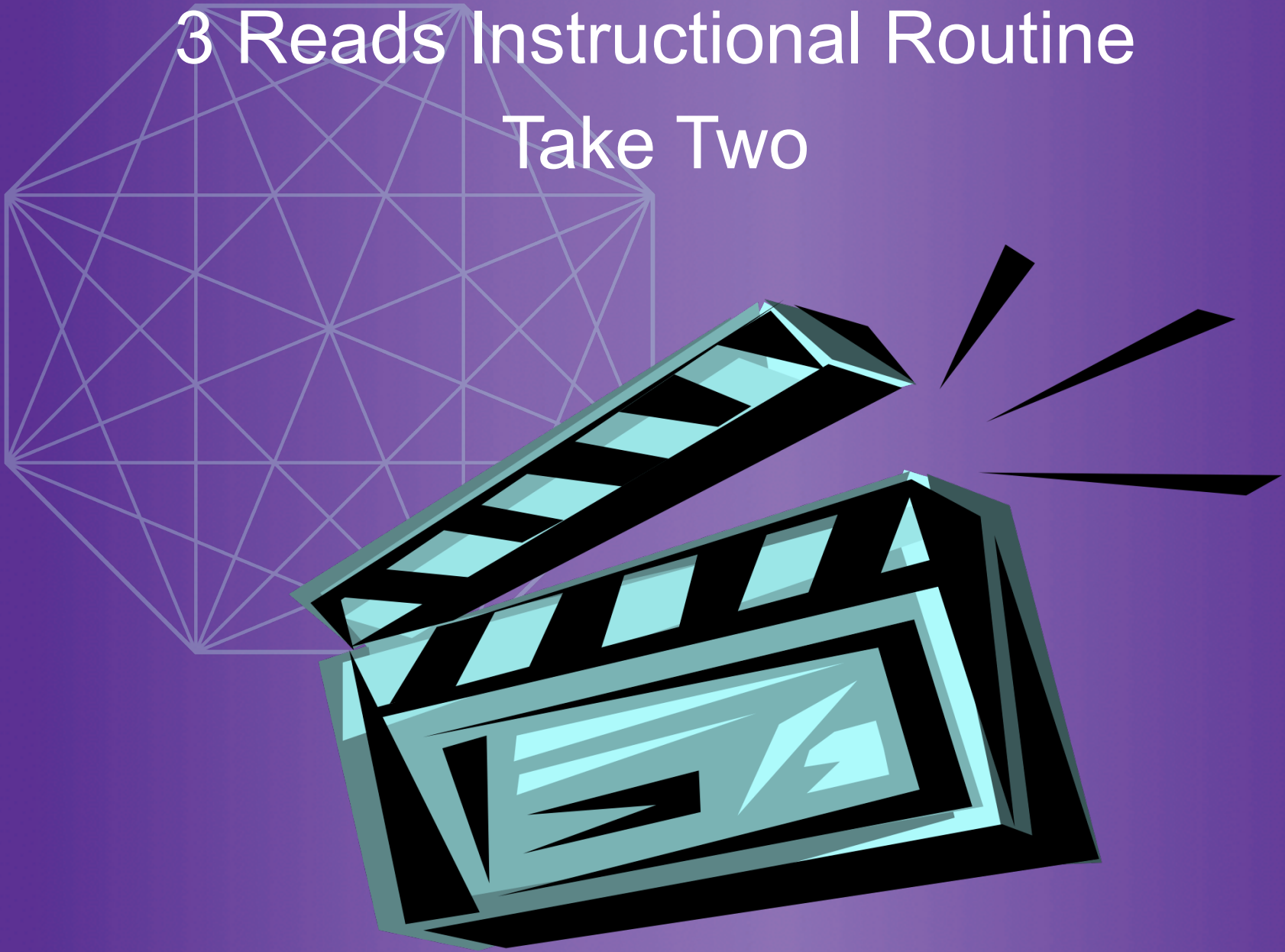


# REFLECT ON 'READING LIKE A MATHEMATICIAN'

- When interpreting a word problem, I learned to ask myself \_\_\_\_\_.
- The next time I read a word problem, I will pay attention to \_\_\_\_\_ because \_\_\_\_\_.

# 3 Reads Instructional Routine

## Take Two

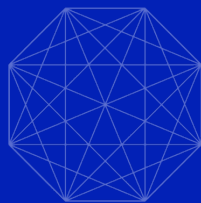




# Three Reads

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An Instructional Routine to Develop  
Reading Like a Mathematician



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# Lesson Goal

Learn to “read like a mathematician”.

Pay attention to quantities in the problem statement.



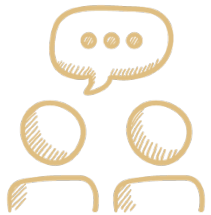
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# 1<sup>st</sup> Read

What is the  
problem  
about?

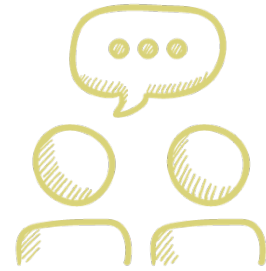


# 2<sup>nd</sup> Read



# What's the Question?

Alicia, Emma, and Nick dive into an extremely deep pool. Alicia dives to a depth of  $-9/4$  meters from the surface of the pool. Emma's depth is twice as far from the surface as Alicia's dive. Nick's depth is  $2/3$  the depth of Alicia's dive.



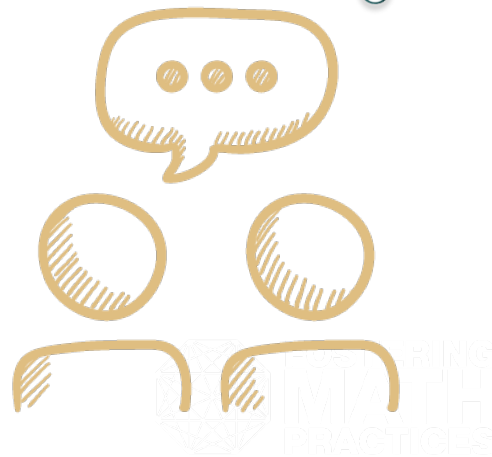
State the question in your own words.

What quantity am I trying to find?



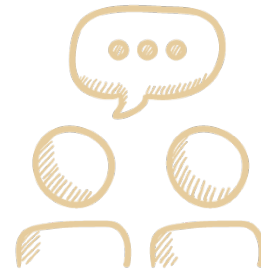
# 3<sup>rd</sup> Read

What's the  
important  
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# What's the Important Information?

Alicia, Emma, and Nick dive into an extremely deep pool. Alicia dives to a depth of  $-9/4$  meters from the surface of the pool. Emma's depth is twice as far from the surface as Alicia's dive. Nick's depth is  $2/3$  the depth of Alicia's dive.



What are the important quantities?

The number of...

# REFLECT ON 'READING LIKE A MATHEMATICIAN'

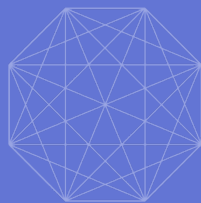
- When interpreting a word problem, I learned to ask myself \_\_\_\_\_.
- The next time I read a word problem, I will pay attention to \_\_\_\_\_ because \_\_\_\_\_.



# Three Reads

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What was the same each time?



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# Structure of the 3 Reads Routine

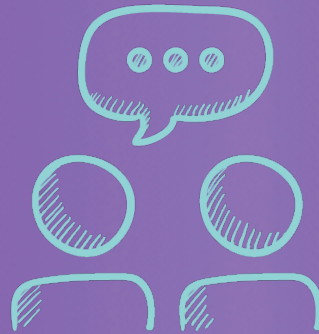
READING GOAL: Read Like a Mathematician



# Next Steps

- REPRESENT the SITUATION
  - Model with manipulatives
  - Represent the problem visually
  - Write a number sentence
  - Write an algebraic expression or equation
- SOLVE the PROBLEM
- REFLECT on reading like a mathematician

# What kind of learner does this way of making sense of a problem situation (MP1) support?



# Consider Ryan

**Ryan** has difficulty with reading comprehension and struggles to distinguish minor details from important information. He benefits from reading a passage multiple times. Ryan is most successful when content is directly connected to his own experiences. He learns best when provided with multiple examples and models.





COULD YOU PLEASE SHOVEL THE RAMP?

ALL THESE OTHER KIDS ARE WAITING TO USE THE STAIRS. WHEN I GET THROUGH SHOVELING THEM OFF, THEN I WILL CLEAR THE RAMP FOR YOU.

BUT IF YOU SHOVEL THE RAMP, WE CAN ALL GET IN!

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[Avenues of Thinking](#)   [Special Populations](#)   [Routines for Reasoning](#) ▾   [Related Resources](#) ▾

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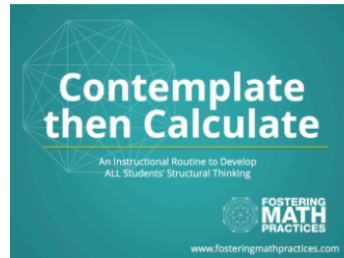
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[View Tasks](#)

Classroom Planner



Classroom PPTX Template



Tasks & Discussion



# For More on Fostering Math Practices through Instructional Routines

## *Reach Out*

GraceKelemanik@gmail.com  
AmyLucenta@gmail.com

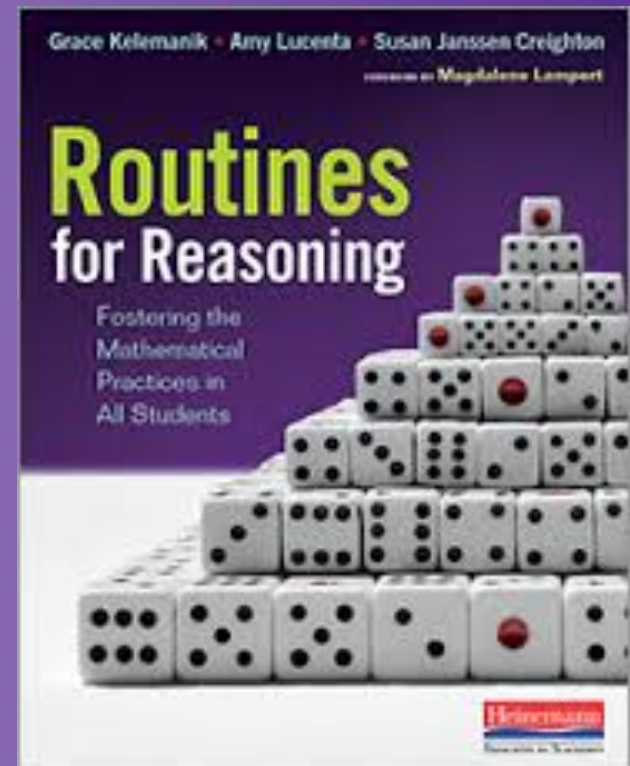
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## *Get the Book!*



# Please provide feedback

## OnebyOne 2017 Session Feedback

\* Required

Session Date \*

- Tuesday, August 15
- Wednesday, August 16
- Thursday, August 17

NEXT